

Connecting  
our communities

Structural Health Monitoring Workshop



Data collection &  
analysis

Nicholas Haritos



ENGINEERS  
AUSTRALIA




SWINBURNE  
UNIVERSITY OF  
TECHNOLOGY



THE UNIVERSITY OF  
MELBOURNE

Proud marketers of the TechnoLab series of  
mechanics teaching products  
**TechnoLab**<sup>TM</sup>  
[www.atrucomp.com](http://www.atrucomp.com)




Tell me, & I will forget.  
Show me, & I may remember.  
Involve me & I will understand.  
(Confucius, circa 450BC)

**"Straight" Lecture/Talk**

**"Illustrated" Lecture/Demo**

**"Hands-on" Practice !**

SHM Workshop - Data collection and analysis  
16/07/2018    Nicholas Haritos



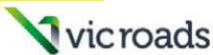
# Outline

## Vibration Based

- What data to collect ?
  - How much to collect ?
  - When to collect data ?
  - Where to collect data ?
- Analysis Options

SHM Workshop - Data collection and analysis  
16/07/2018

Nicholas Haritos




# What data to collect ?



**Aging  
Bridge  
Population**  
→ damage  
→ degradation → monitoring

SHM Workshop - Data collection and analysis  
16/07/2018

Nicholas Haritos



## What data to collect ?

Depends on **Why** you want it &  
**What** you expect to get from it !  
**It's Purpose !**

- Structural Degradation
- Structural Damage
  - *Detection*
  - *Location*
  - *Degree of Severity*
- Effectiveness of a Retrofit, etc

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## What data to collect ?

$F(t) \rightarrow \text{Struct Props} \rightarrow x(t)$

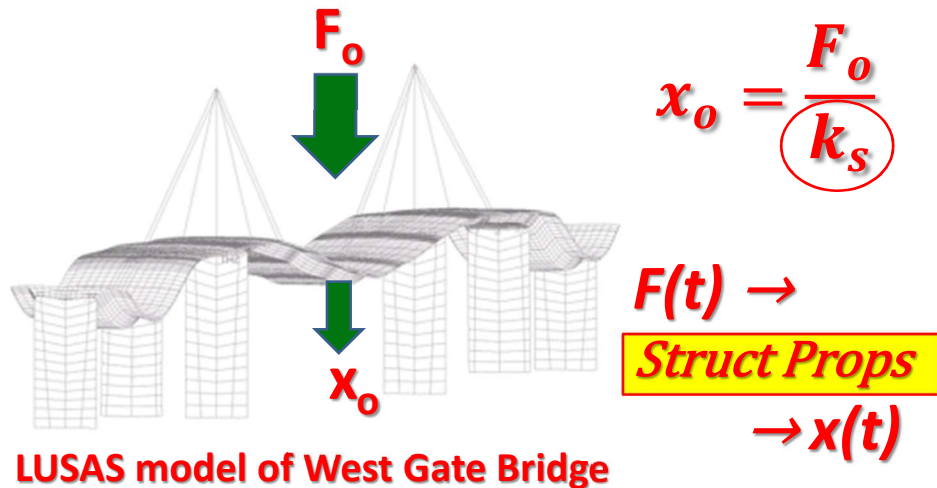
To experimentally determine the **Structural Properties** associated with the transformation of input  $F(t)$  to produce output  $x(t)$  for a particular structure would require measurement of both  $x(t)$  and  $F(t)$  OR the **optimal fitting of theoretical models for this transformation for output only  $x(t)$  measurements\***.

*\*Need make assumptions about properties of the force  $F(t)$*

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## What data to collect ?



SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## Pre-empt Analysis Methods

### *Time Domain based*

- *Auto-Regressive Moving Average (ARMA)*
- *Auto-Regressive Moving Average Vector (ARMAV)*
- *Random Decrement (RANDEC)*

Simultaneous, contemporaneous data capture  
over all response points on grid

### *Frequency Domain based*

- *Mode frequency, damping, mode-shape (& variants)*
- *Frequency Response Function FRF (& variants)*

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



# Modal Analysis

## Computer Packages

$$KX + M \ddot{X} = 0$$

$$\text{Let } X = \phi e^{-i\omega t} \rightarrow \ddot{X} = (-i\omega)^2 \phi e^{-i\omega t}$$

$$KX + M \ddot{X} = (K - \omega^2 M) \phi e^{-i\omega t}$$

$$\rightarrow (K - \omega^2 M)X = 0$$

$$\text{Now: } X = \phi e^{-i\omega t} \neq 0$$

$$\therefore |(K - \omega^2 M)| = \det((K - \lambda M)) = 0$$

$\lambda$  – *eigenvalue*

$\phi$  – *eigenvector*

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



$$F(t) \rightarrow \boxed{\text{Struct Props}} \rightarrow x(t)$$

## Modal Analysis – Computer Progs.


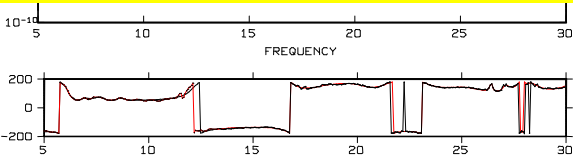


etc . . . . .

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos

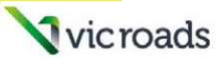


# Experimental Modal Analysis

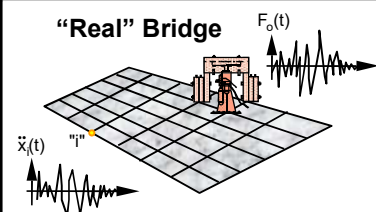

$$\min_{\{\lambda_s, \phi_{jn}\}} \sum_{\omega=\omega_{\min} \dots \omega_{\max}} \left( \sum_k \left( \sum_{j=1}^N \left| \tilde{h}_{jk}(\omega) - \sum_{n=1}^M \left( \frac{\phi_{jn} \phi_{kn}}{(i\omega - \lambda_n)} + \frac{\phi_{jn}^* \phi_{kn}^*}{(i\omega - \lambda_n^*)} \right) \right|^2 \right) \right)$$


$\lambda$  – eigenvalue       $\phi$  – eigenvector

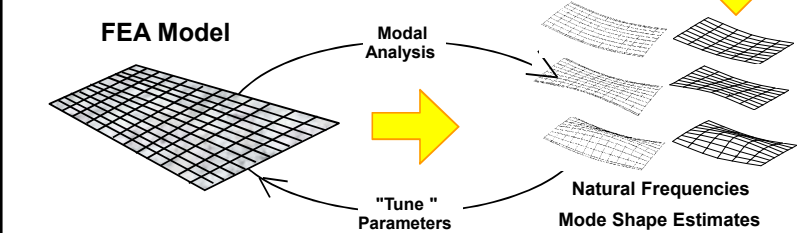
SHM Workshop - Data collection and analysis  
16/07/2018



## “Traditional” EMA using a Shaker



$$FRF_{io}(\omega) = \frac{F_{\ddot{x}_i}(\omega)}{F_{F_0}(\omega)}$$

Modal Extraction (DSMA)



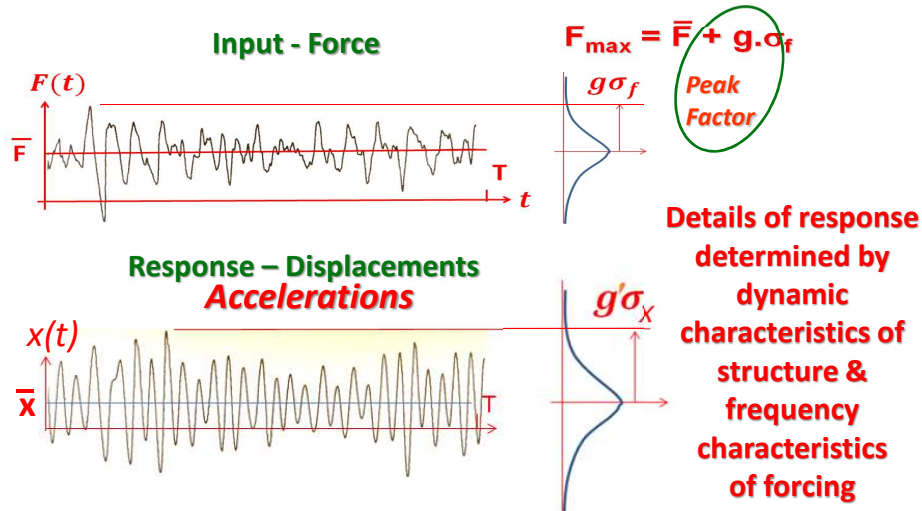
FEA Model      Modal Analysis      Natural Frequencies  
Mode Shape Estimates      "Tune " Parameters

SHM Workshop - Data collection and analysis  
16/07/2018





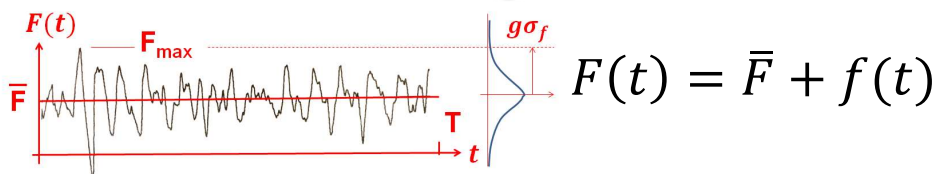
## What data to collect ?



SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## Modelling Stochastic (Random-like) Forcing



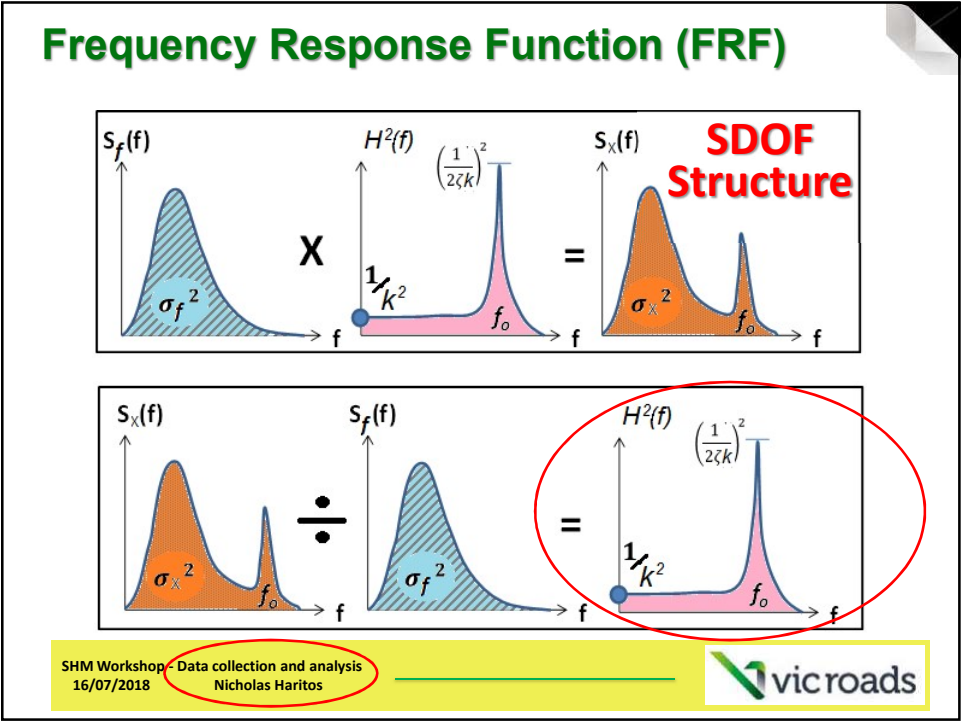
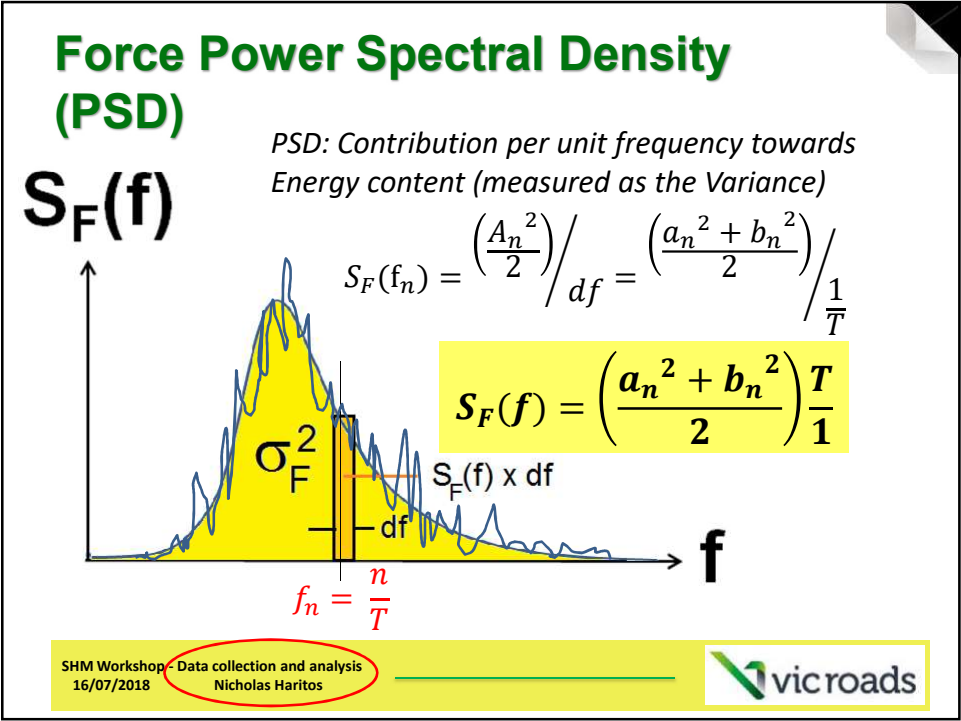
$$f(t) = \sum_{n=0}^{\infty} \left( a_n \cos \left( \left( \frac{2\pi n}{T} \right) t \right) + b_n \sin \left( \left( \frac{2\pi n}{T} \right) t \right) \right)$$

$$f(t) = \sum_{n=0}^{\infty} A_n \cos \left( \left( \frac{2\pi n}{T} \right) t - \phi_n \right) = \sum_{n=0}^{\infty} A_n \cos(2\pi f_n t - \phi_n)$$

$$\sigma_f^2 = 0 + \sum_{n=0}^{\infty} \left( \frac{a_n^2}{2} \right) + \sum_{n=0}^{\infty} \left( \frac{b_n^2}{2} \right) = \sum_{n=0}^{\infty} \left( \frac{a_n^2 + b_n^2}{2} \right)$$

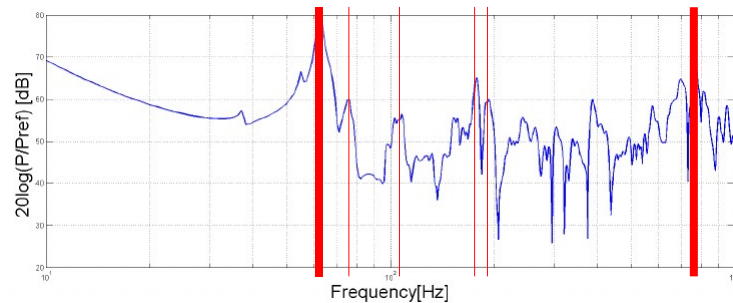
SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos







# FRF



**Lowest Frequency  
of Interest,  $f_o$**

**Highest Frequency  
of Interest,  $f_H$**

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



# Outline

## Vibration Based

- What data to collect ?
  - How much to collect ?
  - When to collect data ?
  - Where to collect data ?
- Analysis Options

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



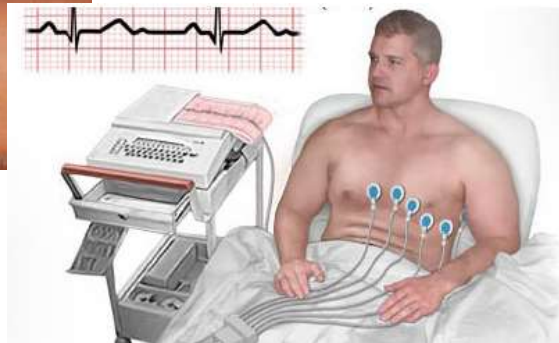
## How much/when to collect?

- Sampling Rate,  $f_s$  of data must be  $> 2 * f_H$
- Minimum Sampling Rate suggest be  $> 3 * f_H$
- Preferred Sampling Rate of Data  $> 5 * f_H$
- Suggested frequency of resolution,  $< \alpha f_o$   
 $df < 1/T = \alpha f_o$ , eg  $\alpha$  of 1%  $\rightarrow T > 100/f_o$
- Number of data points/record  $N = T * f_s = f_s / (\alpha f_o)$   
 eg for:  $f_s = 4 * f_H$ ,  $\alpha$  of 1%  $\rightarrow N = 4f_H / (\alpha f_o)$   
 for  $f_H / f_o = 10$  (say  $f_o = 8\text{Hz}$ )  $\rightarrow N = 4,000$  points  
 (Useful if using EXCEL for  $N = 4096$  - largest power of 2 for FFT algorithm in EXCEL)

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## What data to collect ?




SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



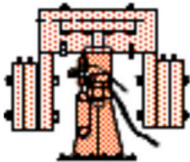

# What data to collect ?


## Input - Force




Instrumented impact hammer

Virtually impossible to measure except if structure (bridge) closed to traffic & using a Controlled Shaker





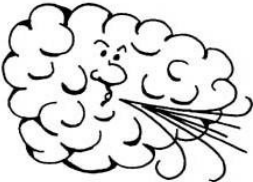



SHM Workshop - Data collection and analysis  
16/07/2018

vicroads


# What data to collect ?

## Input – Forcing Unmeasured





Natural Traffic



SHM Workshop - Data collection and analysis  
16/07/2018

vicroads

# What data to collect ?

## Response – Displacements


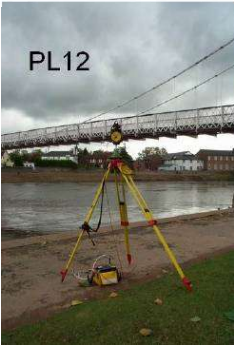
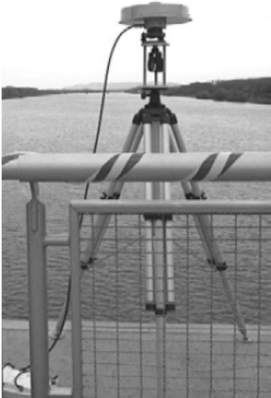


SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



# What data to collect ?


## Response – Displacements



**Pseudolites**  
(~ground satellites) ↑  
*improve accuracy*

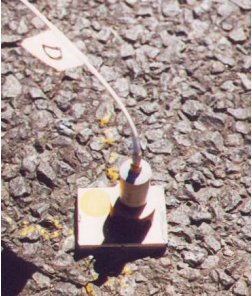

**GPS Measurement Node**

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



# What data to collect ?

Response – Displacements  
**Accelerations**



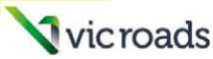
**Dytran accelerometer with magnetic base attachment**

**PCB accelerometer with magnetic base attachment**

**Typical corded accelerometers**

SHM Workshop  
16/07/2018

Data collection and analysis  
Nicholas Haritos



# What data to collect ?

Response – **Accelerations**

## Wireless

**Smart Phones**



Android  
Apple iOS

**External BT Accelerometers**



**GCDC Data-logging Accelerometers**



MEL-X2



X2-2



**Coordinator (WSN Manager)**



Wireless Sensor

Wireless Sensor

Wireless Sensor

Wireless Sensor

**BeanAir**

**Serious Stuff!**

SHM Workshop  
16/07/2018

Data collection and analysis  
Nicholas Haritos





# What data to collect ?

Response – **Measurement**



(a) 16-channel 20mA constant current power supply



(b) NI - SCXI Signal Conditioning Unit



(c) NI – based DAS using 16-bit ADDA and a notebook computer

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## Outline

### Vibration Based

- What data to collect ?
  - When to collect data ?
  - How much to collect ?
  - **Where to collect data ?**
- Analysis Options

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos





# Where to collect data?

Depends on **Why** you want it &  
**What** you expect to get from it !  
**It's Purpose !**

- Structural Degradation
- Structural Damage Detection
  - Location
  - Degree of Severity
- Effectiveness of a Retrofit, etc

→ **Fine grid**

SHM Workshop - Data collection and analysis  
16/07/2018

vicroads

# Where to collect data?

## Narrow/Cantilever Bridges

- Response modes largely flexural & torsional
- Can use **two lines of edge nodes** as a minimal grid

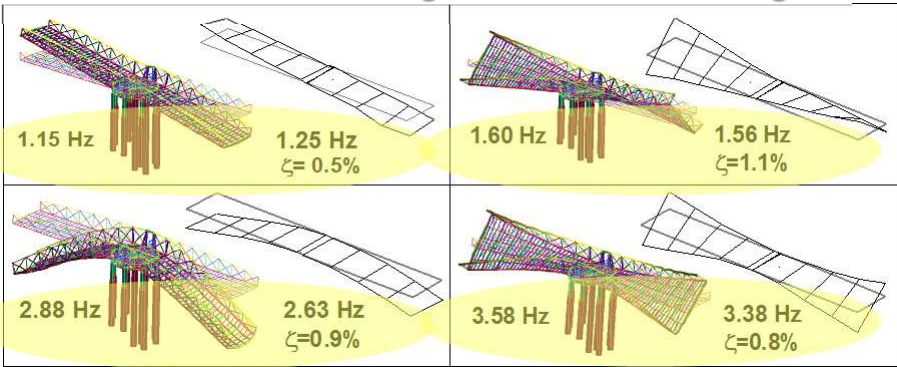
SHM Workshop - Data collection and analysis  
16/07/2018

vicroads

# Where, to collect data ?

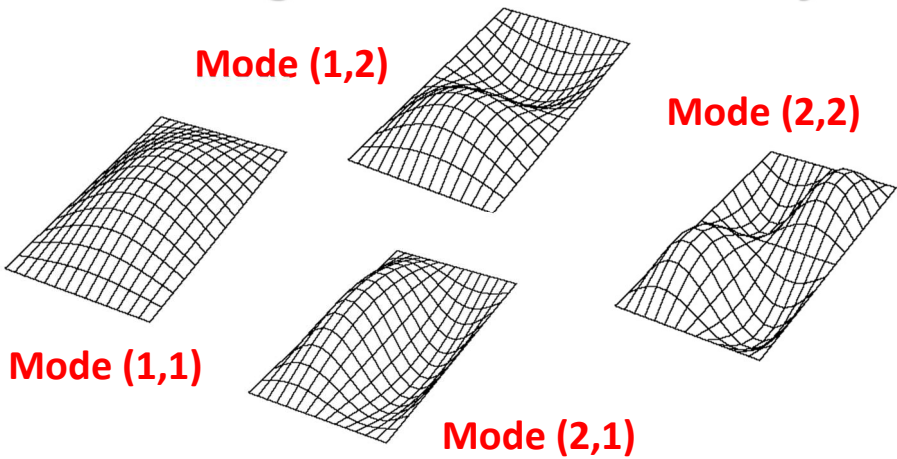
## Narrow/Cantilever Bridges

- Response modes largely flexural & torsional
- Can use two lines of edge nodes as a minimal grid



# Plate-like behaviour

→ Fine grid becomes necessary

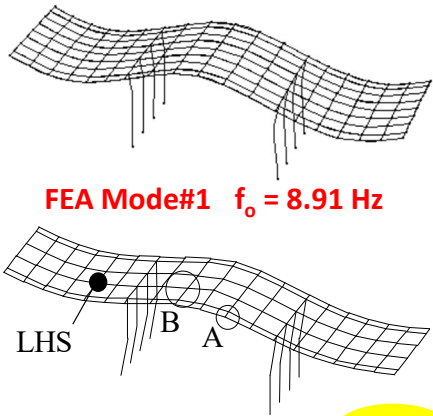


# Example Grids (EMA)



**Congongella Creek Bridge**

**Congongella Creek Bridge: Mode#1**



SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos

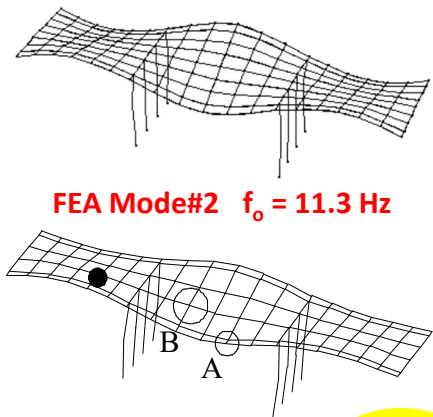


# Example Grids (EMA)



**Congongella Creek Bridge**

**Congongella Creek Bridge: Mode#2**



SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos

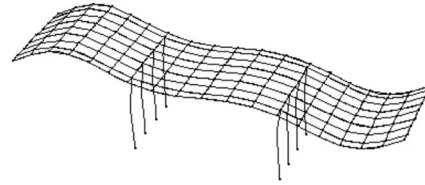


## Example Grids (EMA)

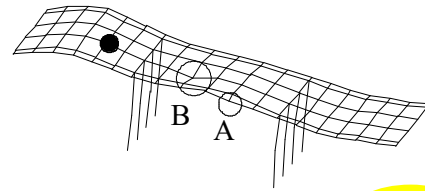


Concongella Creek Bridge

Concongella Creek Bridge: Mode#3



FEA Mode#3  $f_o = 12.6 \text{ Hz}$



EMA Mode#3  $f_o = 13.0 \text{ Hz}$   $\zeta = 12.3\%$

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## Outline

### Vibration Based

- What data to collect ?
  - When to collect data ?
  - How much to collect ?
  - Where to collect data ?
- Analysis Options

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



# Analysis Options

Depends on **Why** you want it &  
**What** you expect to get from it !  
**It's Purpose !**

- Structural Degradation
- Structural Damage Detection
- Effectiveness of a Retrofit, etc

Simple EMA

→ Tier#1

'Ambient' EMA

→ Tier#2

Traditional EMA

→ Tier#3

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## Simple EMA → Tier#1

Single Point Monitoring →

- Can determine dominant (modal) frequencies
- In conjunction with an EMA model may be able to infer participation of detected modes
- May be sufficient to infer "all is well"

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos





## **‘Ambient’ EMA → Tier#2**

### **Multi- Point Monitoring →**

- **Can determine dominant (modal) frequencies**
- **Can obtain Operational Deflected Shapes  
~ mode shapes when freqs. separated**
- **May be sufficient to infer “possible” deterioration and/or damage**

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## **‘Traditional’ EMA → Tier#3**

### **Multi- Point Monitoring →**

- **Can determine dominant (modal) frequencies and damping**
- **Can determine mode shapes even when modes may be closely spaced in frequency**
- **Provide the basis for damage identification, location and its extent, more . . . .**

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos





# Software

- **Purpose-specific “research” style software possessed by several universities**

**Data Acquisition System (DAS) with  
Simultaneous Sample and Hold, and  
anti-aliasing filters,  
→ 16-channel Spectral Analyser**

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



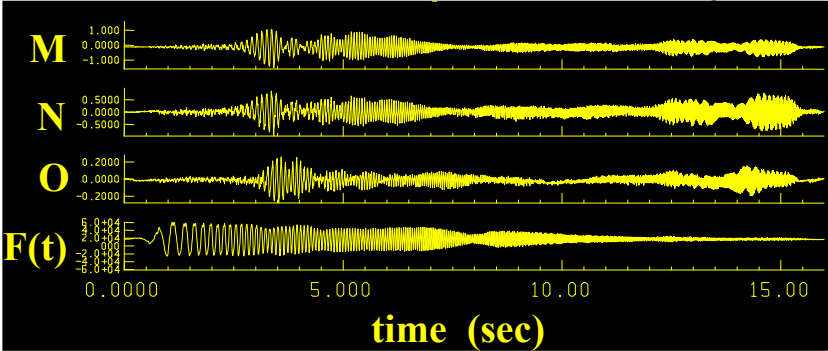
# Research Software



SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



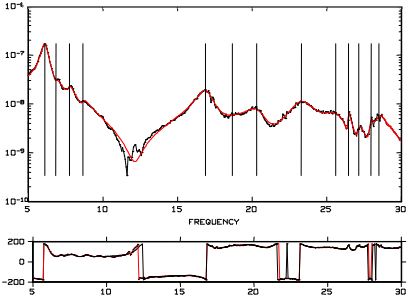
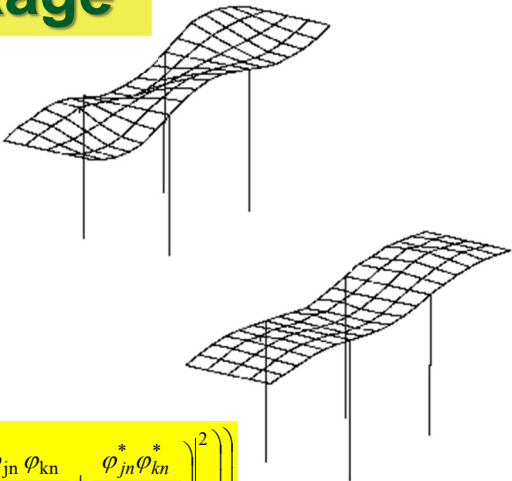
# Software



SHM Workshop - Data collection and analysis  
16/07/2018

vicroads

# DSMA Package


$$\min_{\{\lambda_n, \varphi_{jn}\}} \sum_{\omega=\omega_{\min} \dots \omega_{\max}} \left( \sum_k \left( \sum_{j=1}^N \left| \tilde{h}_{jk}(\omega) - \sum_{n=1}^M \left( \frac{\varphi_{jn} \varphi_{kn}}{(i\omega - \lambda_n)} + \frac{\varphi_{jn}^* \varphi_{kn}^*}{(i\omega - \lambda_n^*)} \right) \right|^2 \right) \right)$$

SHM Workshop - Data collection and analysis  
16/07/2018

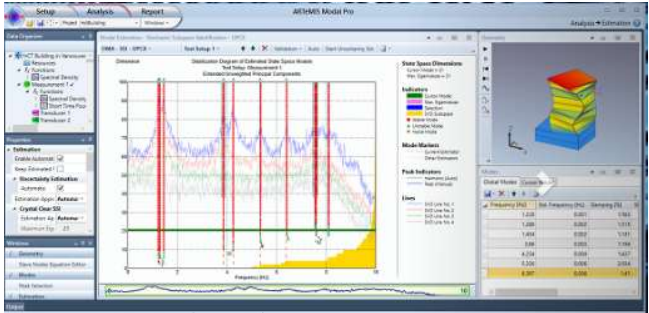
vicroads

# Commercial Software



## ARTEMIS Modal Product Information

- Operational Modal Analysis (OMA)
- Experimental Modal Analysis (EMA)
- Operating Deflection Shape Analysis (ODS)
- Structural Health Monitoring (SHM)



SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



# Commercial Software



**ME'scope VES**  
Visual Engineering Series

- ODS Animation
- FRF-Based Modal Analysis
- Operational Modal Analysis
- Vibro-Acoustic Analysis
- Dynamics Modeling & Simulation
- Structural Dynamics Modification
- FEA Model Updating

SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos







SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos

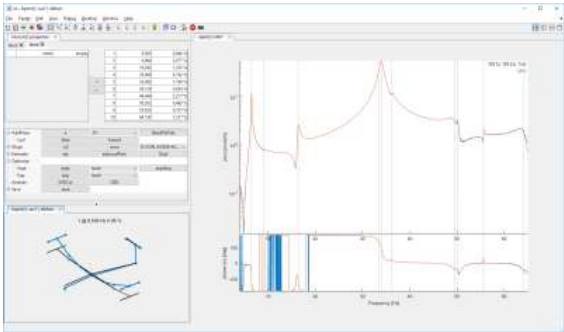


# Commercial Software


**SD Tools**  
VIBRATION SOFTWARE & CONSULTING

## Experimental Modal Analysis

### Frequency domain identification



SHM Workshop - Data collection and analysis  
16/07/2018 Nicholas Haritos



## Commercial Software



<http://www.realvibrations.com/>

### Australian Product

**Multi-axis Vibration Shaker Controllers;** Field Data Analyser

**Multi-channel Real-time Signal Recorder;**

**Multi-channel Signal Analyser**

**Dual-channel Spectrum Analyser - Impact Excitation**

**Dual-channel Spectrum Analyser - Random Excitation**

**Cushion / Impact Analyser**

**Vibration Fatigue Analyser; Seismic Motion Analyser**

SHM Workshop - Data collection and analysis  
16/07/2018  
Nicholas Haritos

