

14<sup>th</sup> Annual Workshop for Australian Network of Structural Health Monitoring

# Damage Detection Using Nonlinear Ultrasonic Guided Waves

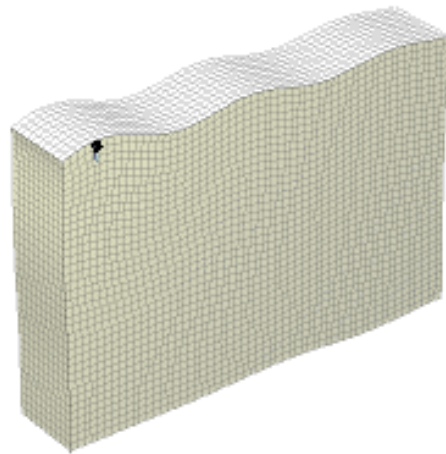
Prof. (Alex) Ching-Tai Ng



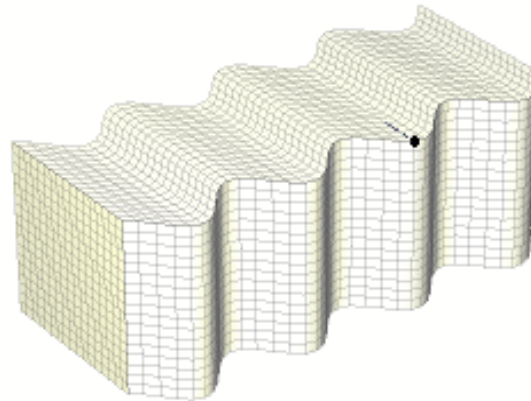
# Ultrasonic Guided Waves

Ultrasonic guided waves propagate in solid media, interacting with boundaries in such a way that boundary conditions could be satisfied.

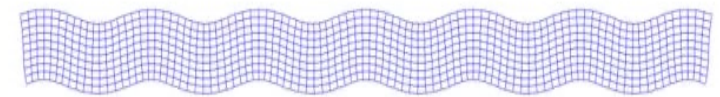
- Sensitive to small and different types of damages
- Relatively long travel distance
- Inaccessible location of structures can be inspected



Rayleigh Wave



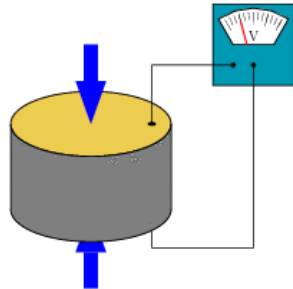
Shear Horizontal  
Wave



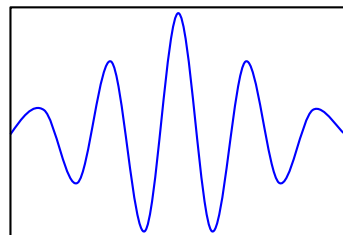
Lamb Wave

# Ultrasonic Guided Waves

- Guided Wave Modes



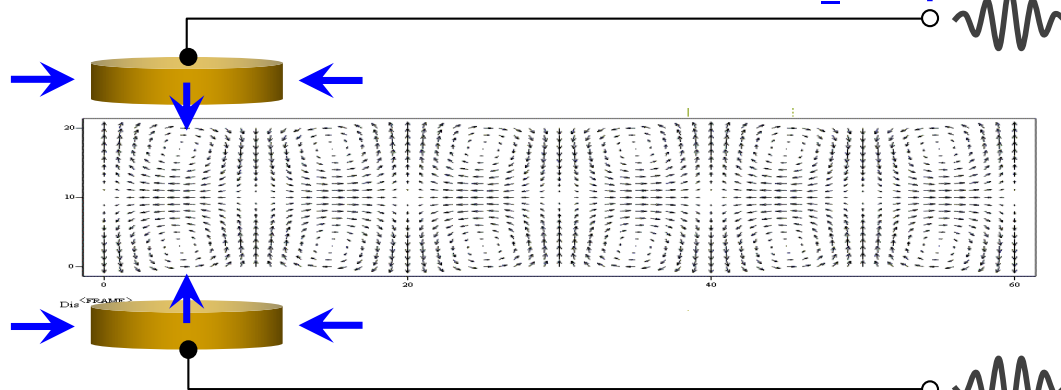
Piezoceramic transducer



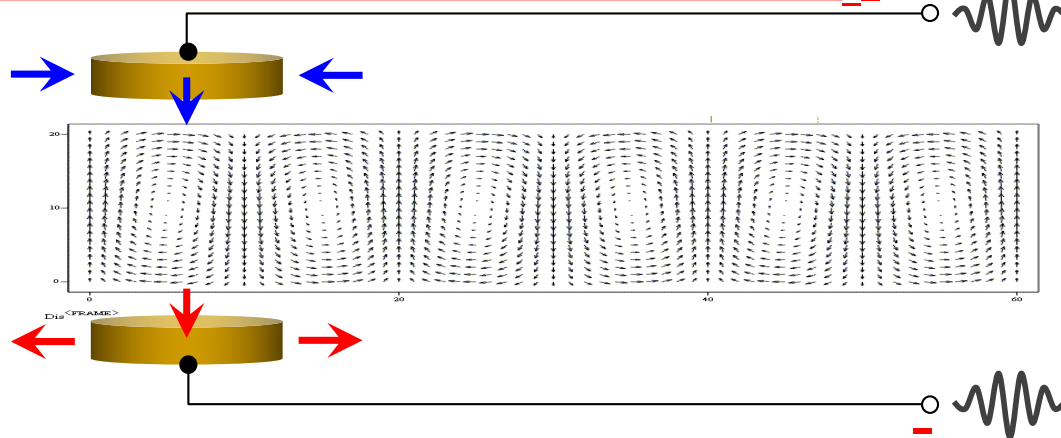
Hanning windowed sinusoidal tone burst

Slide 2 pulse

## Fundamental symmetric mode ( $S_0$ )



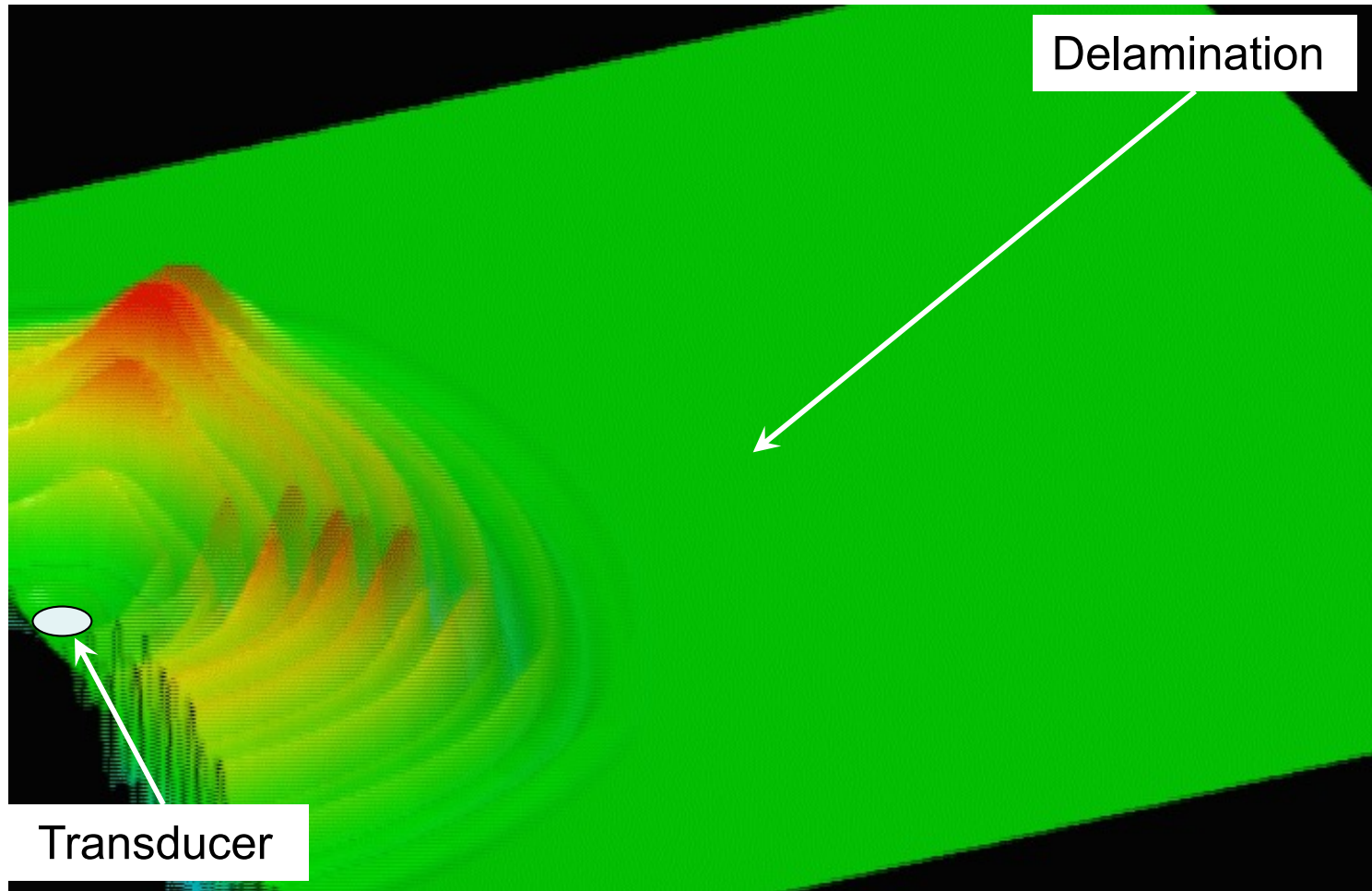
## Fundamental anti-symmetric mode ( $A_0$ )



Giurgiutiu & Bao (2004) *Struct. Health. Monitor.* Animation from [\[www.me.sc.edu/Research/lamss/\]](http://www.me.sc.edu/Research/lamss/)

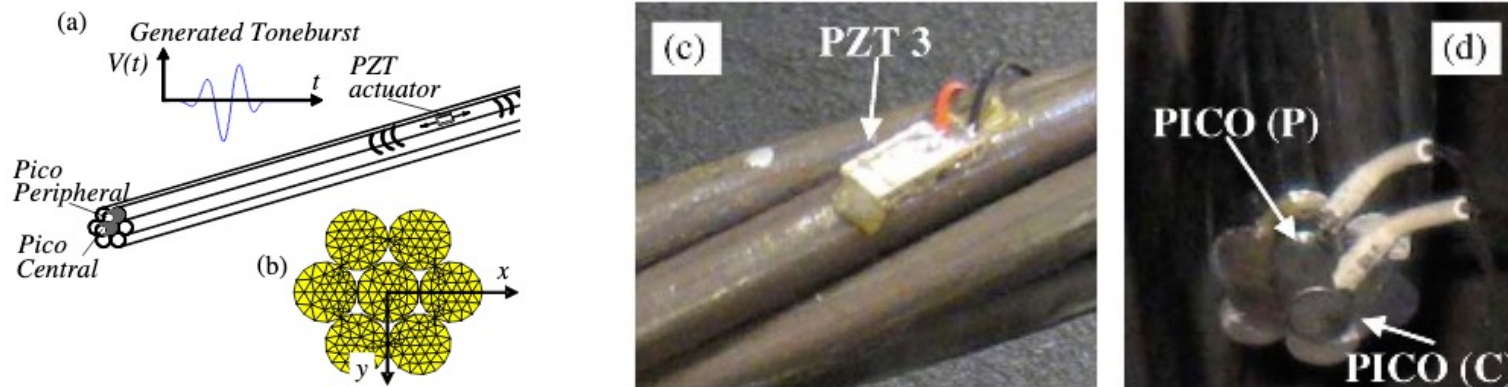
# Guided Waves in Plates (Lamb Waves)

- ❖ Example of guided wave propagation and interact with damage



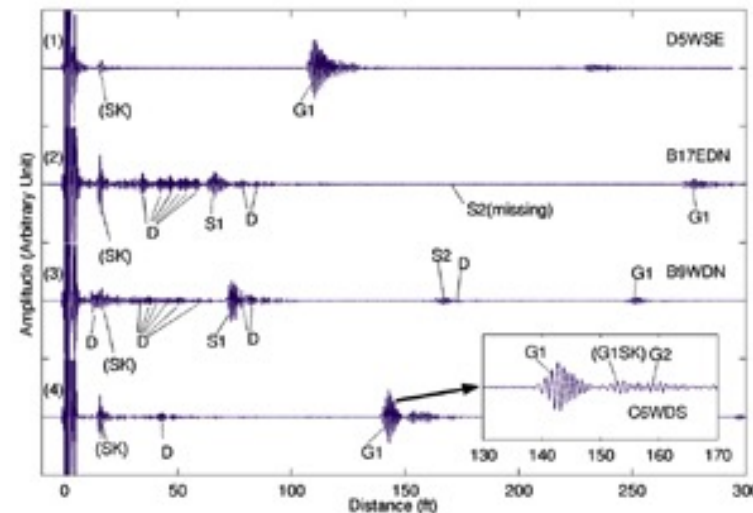
Scaled displacement contour plot

# Applications of Ultrasonic Guided Waves



## Determination of prestress loss in multiwire tendons

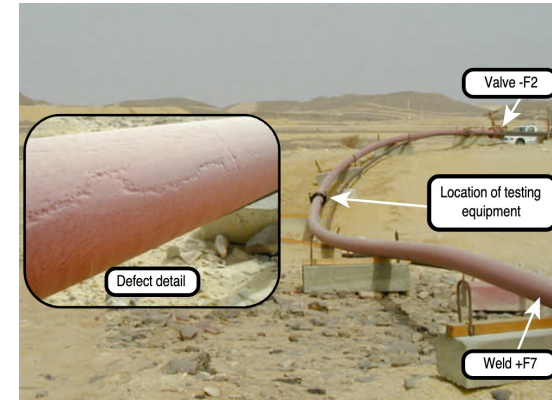
*Bartoli I, Salamone S., Phillips R., Lanza di Scalea F., Sikorsky C.S. (2011). Use of interwire ultrasonic leakage to quantify loss of prestress in multiwire tendons. J. Eng. Mech. ASCE, 137(5):324-333.*



## Inspection of cables in suspension bridge

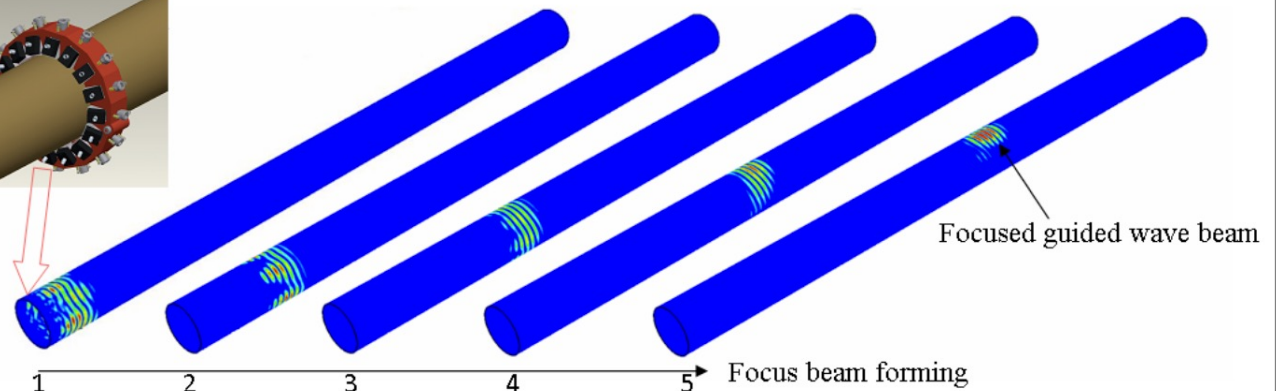
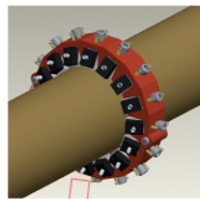
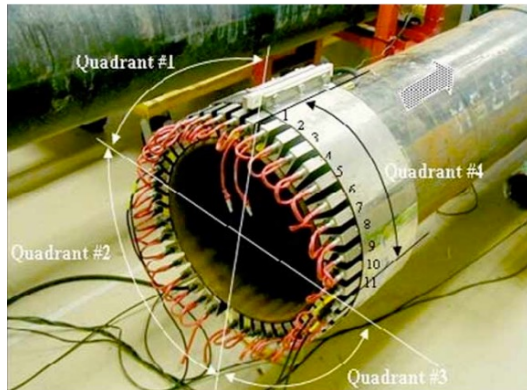
*Kwun H. (2003). Waves of the future, Technology Today, Fall: 16-20.*

# Applications of Ultrasonic Guided Waves



Long range inspection of pipe

*Alleyne D.N., Pavlakovic B., Lowe M.J.S., Cawley P. (2001). Rapid, long range inspection of chemical plant pipework using guided waves. AIP Conf. Proc. 557:180-187.*



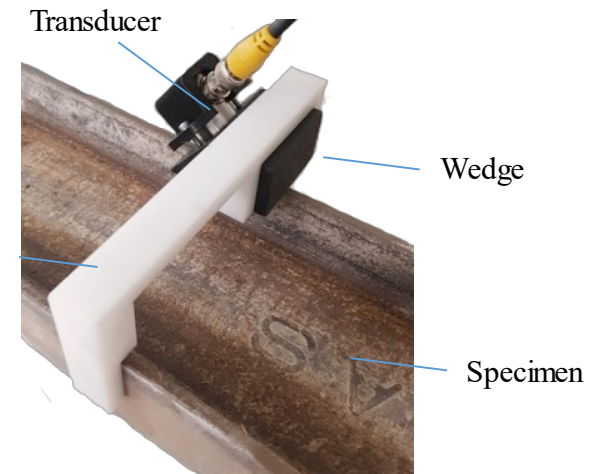
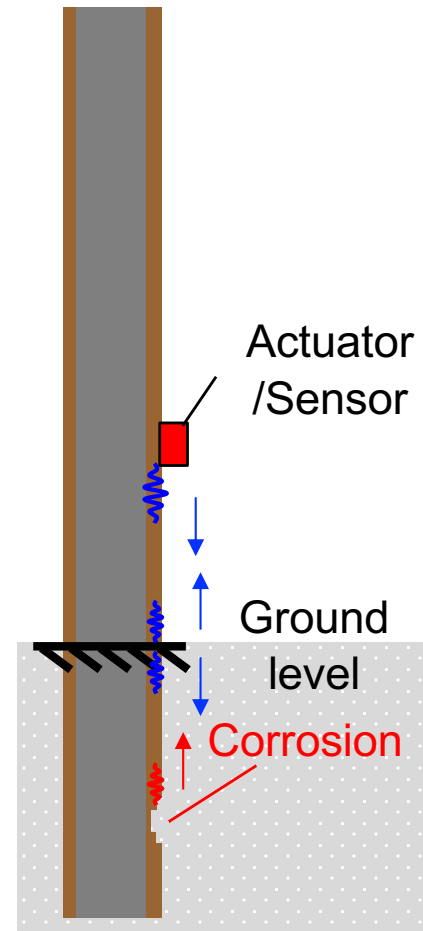
Focused guided wave inspection for pipes

*Mu J., Hua J. Rose J.L. (2010). Ultrasonic guided wave focus inspection potential of bare and coated pipes. AIP Conf. Proc. 1211:239-246.*

# Applications of Ultrasonic Guided Waves

## Corrosion detection at inaccessible location (University of Adelaide)

There are 720,000 Stobie poles in South Australia

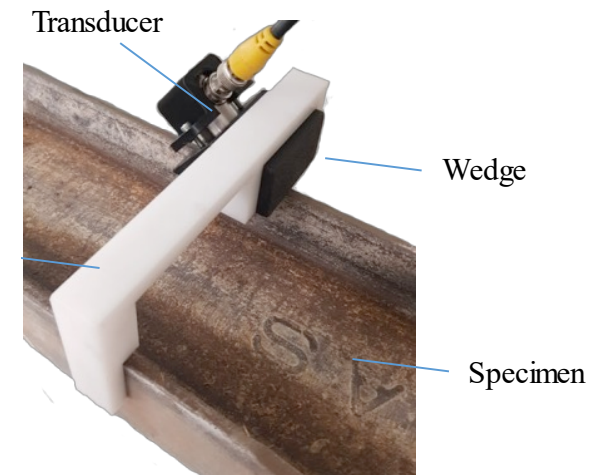
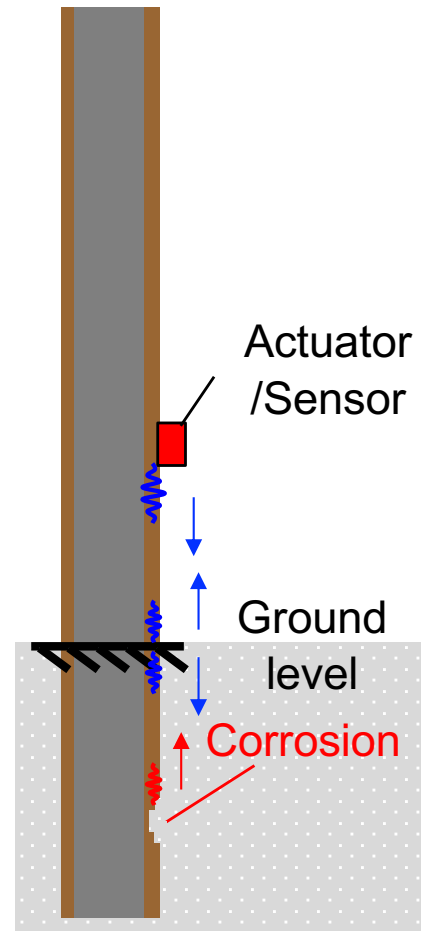
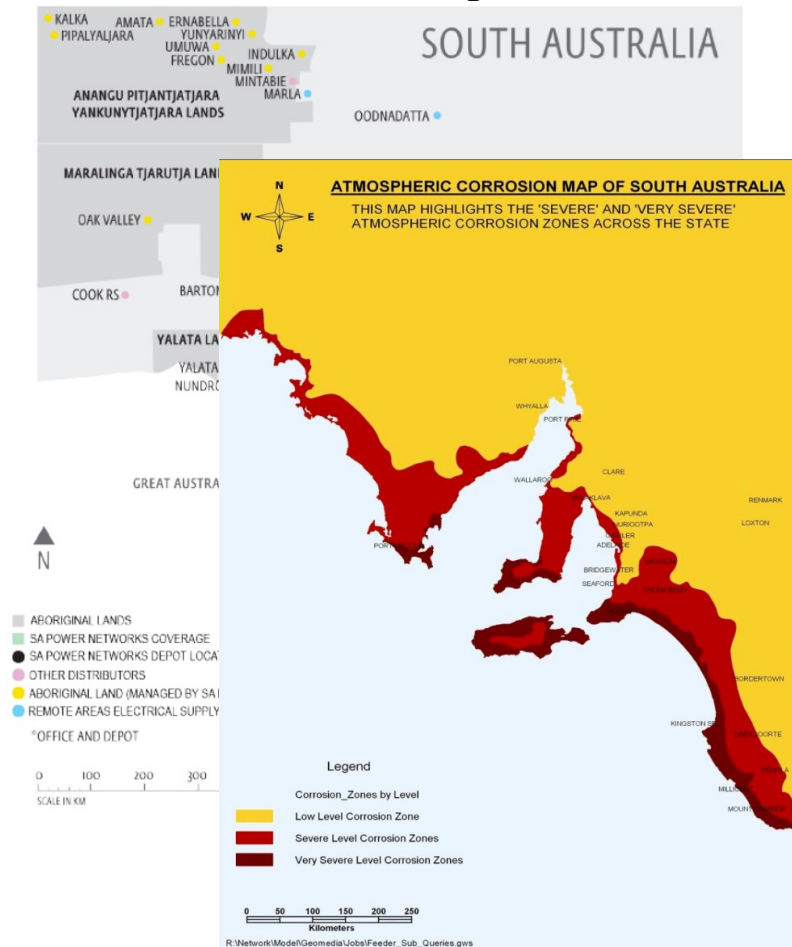


(SA Asset Management Plan 3.1.05 Poles 2014 to 2025 (2014))

# Applications of Ultrasonic Guided Waves

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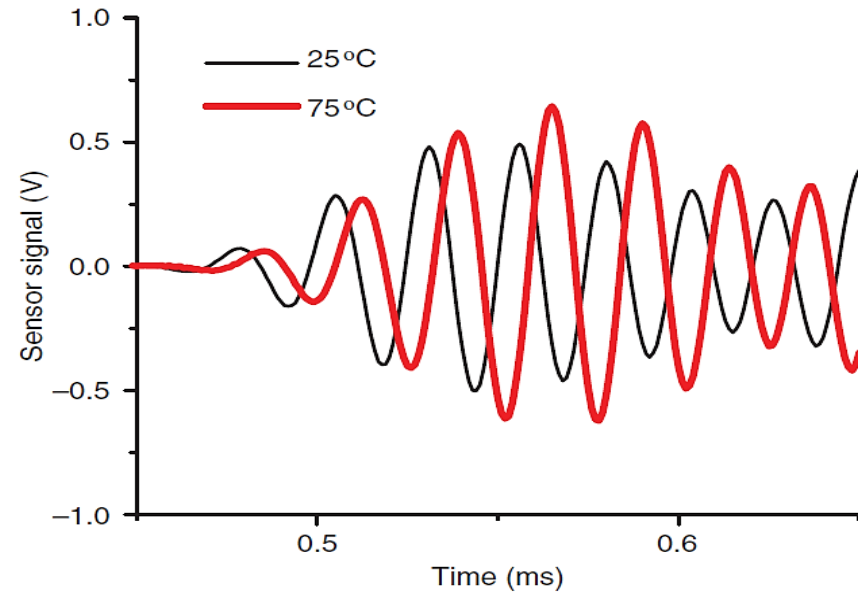
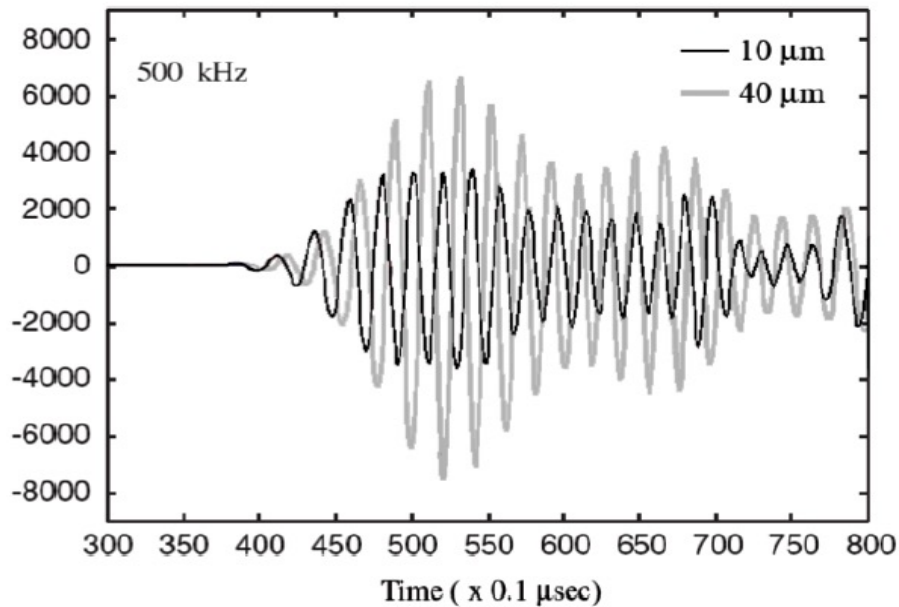


(SA Asset Management Plan 3.1.05 Poles 2014 to 2025 (2014))



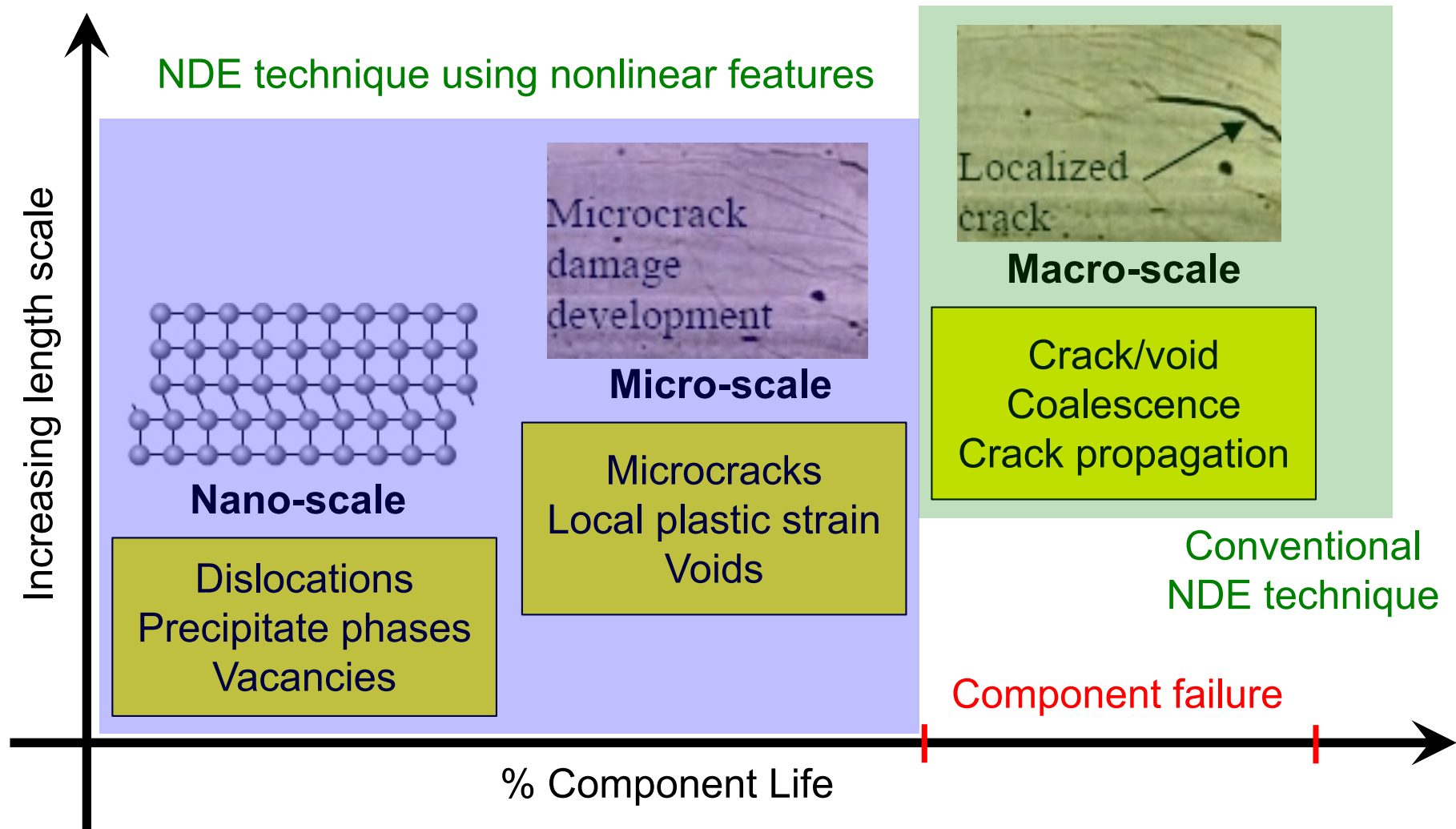
# Limitations of Linear Guided Wave

The effect of adhesive layer thickness change on sensor signals (for 10  $\mu\text{m}$  to 40  $\mu\text{m}$ ) (Ha and Chang 2010)



Temperature effect on PZT sensor signals at  $f=300$  kHz (Ha et al. 2010)

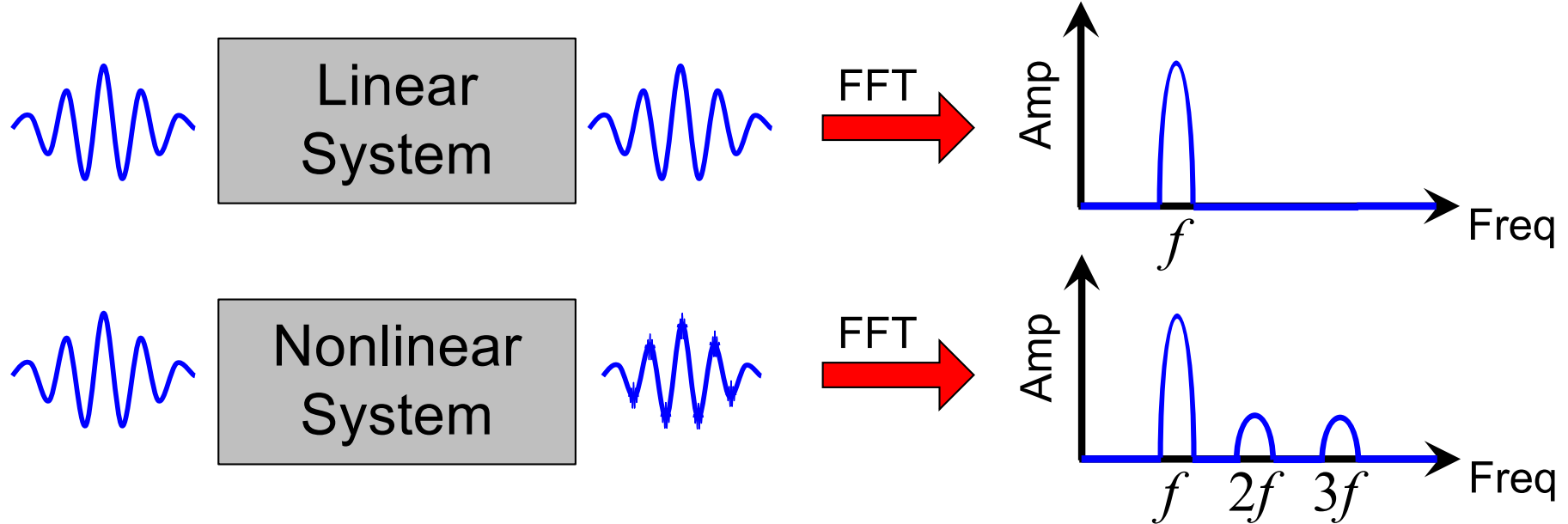
# Nonlinear Guided Wave: Life of Structural Components



- **Microstructural evolution drives macroscopic damage**
- **How can we monitor features at lower length scales?**

# Nonlinear Guided Wave: Higher Harmonic Generation

❖ Higher harmonic generation due to nonlinearities

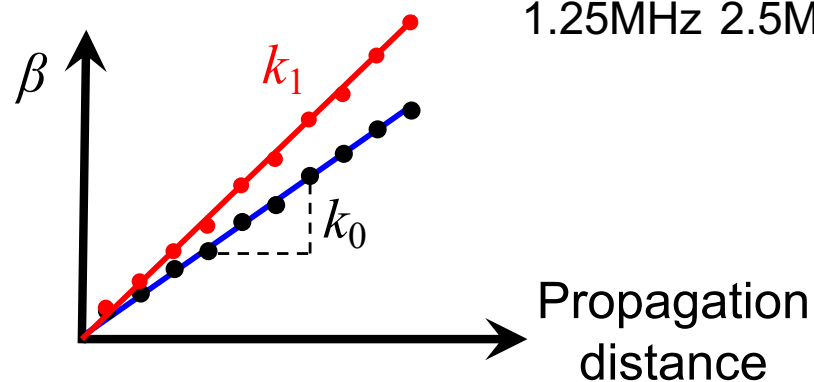
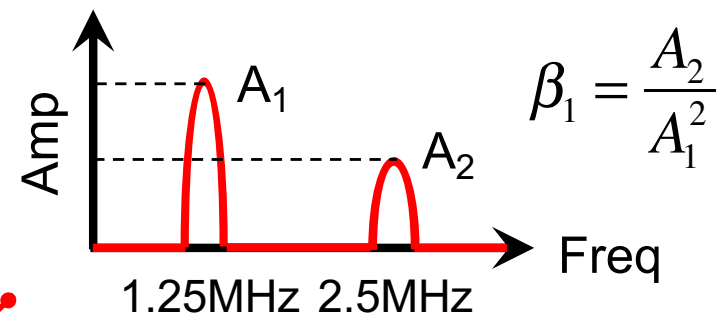
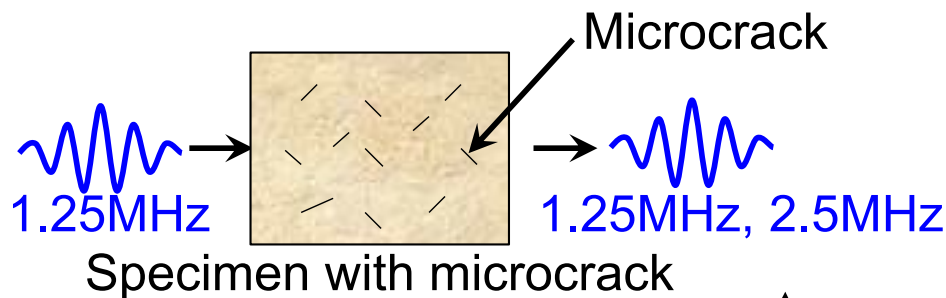
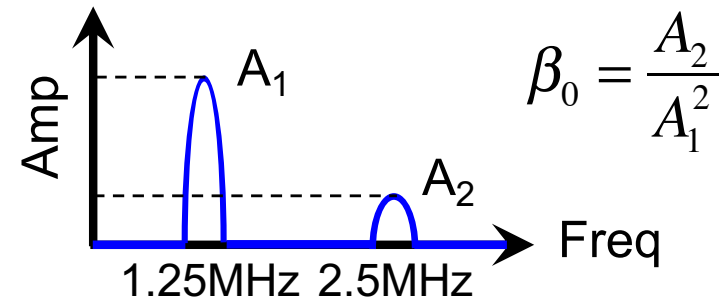
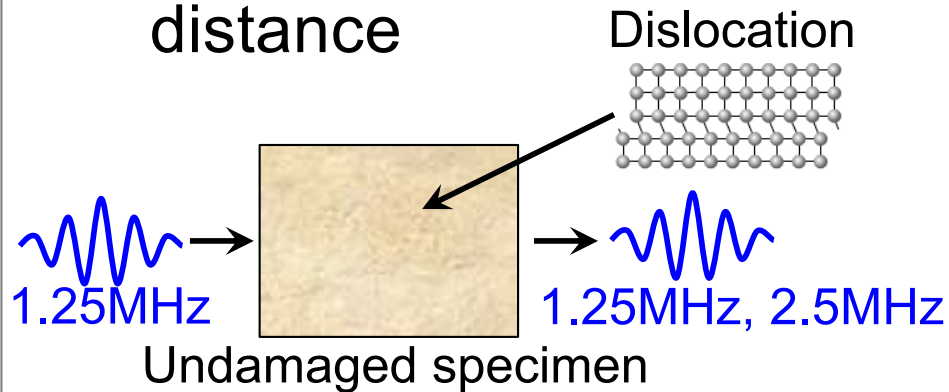


❖ Sources of nonlinearity:

- Material nonlinearity
- Contact nonlinearity
- Equipment, e.g. amplifier
- Transducer
- Structural connections

# Nonlinear Guided Wave: Material Nonlinearity

- When fulfilling specific conditions, accumulative second harmonic is linearly increase with the wave propagation distance



# Advantages and Challenges of Using Nonlinear Guided Waves

## Advantages:

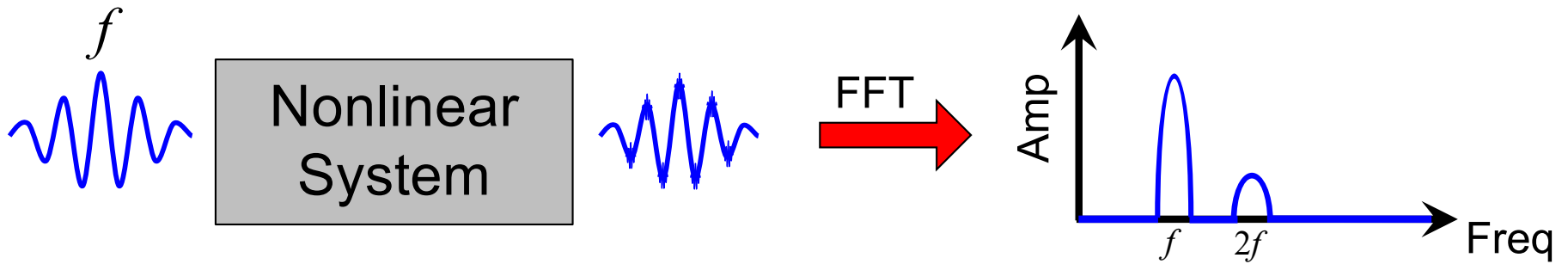
- Higher sensitivity to early-stage damage
- Potential to be a non-baseline damage detection approach

## Challenges:

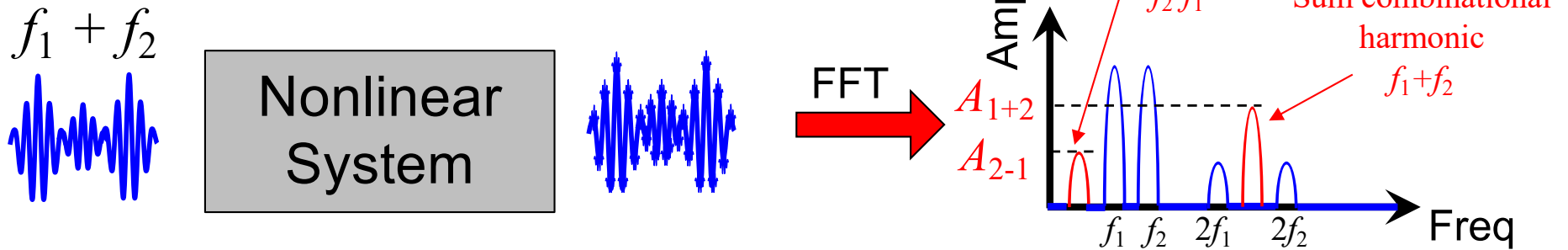
- Extraction of nonlinear features
  - (1) Small magnitude of generated higher harmonic,
  - (2) Damage induced vs non-damage induced nonlinearities

# Ultrasonic Guided Wave Mixing

- **Single frequency nonlinear guided wave**



- **Guided wave mixing**



$$\beta_{sum} = \frac{A_{1+2}}{A_1 A_2}$$

$$\beta_{diff} = \frac{A_{2-1}}{A_1 A_2}$$

# Phase Reversal Approach

Nonlinear wave equation:

$$\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2} + c^2 \beta \frac{\partial u}{\partial x} \frac{\partial^2 u}{\partial x^2}$$

Solution of the nonlinear wave equation:

$$u(x, t) = \underbrace{u_a^{(1)}}_{\text{Linear}} + \underbrace{u_a^{(2)}}_{\text{Nonlinear}} + \underbrace{u_b^{(1)}}_{\text{Linear}} + \underbrace{u_b^{(2)}}_{\text{Nonlinear}}$$

Final solution of displacement field:

$$u(\tau)^{(0^\circ)} = A_a \sin(\omega_a \tau) + A_b \sin(\omega_b \tau)$$

$$- \frac{\beta x}{8c^2} \{ A_a^2 \omega_a^2 \cos 2(\omega_a \tau) + A_b^2 \omega_b^2 \cos 2(\omega_b \tau) + 4A_a A_b \omega_a \omega_b [\cos(\omega_a \tau) \cos(\omega_b \tau)] \}$$

Linear wave components

Nonlinear wave components

Phase reversed displacement field:

$$u(\tau)^{(180^\circ)} = A_a \sin(\omega_a \tau + \pi) + A_b \sin(\omega_b \tau + \pi)$$

$$- \frac{\beta x}{8c^2} \{ A_a^2 \omega_a^2 \cos 2(\omega_a \tau + \pi) + A_b^2 \omega_b^2 \cos 2(\omega_b \tau + \pi) + 4A_a A_b \omega_a \omega_b [\cos(\omega_a \tau + \pi) \cos(\omega_b \tau + \pi)] \}$$

# Phase Reversal Approach for Extracting Higher Harmonic

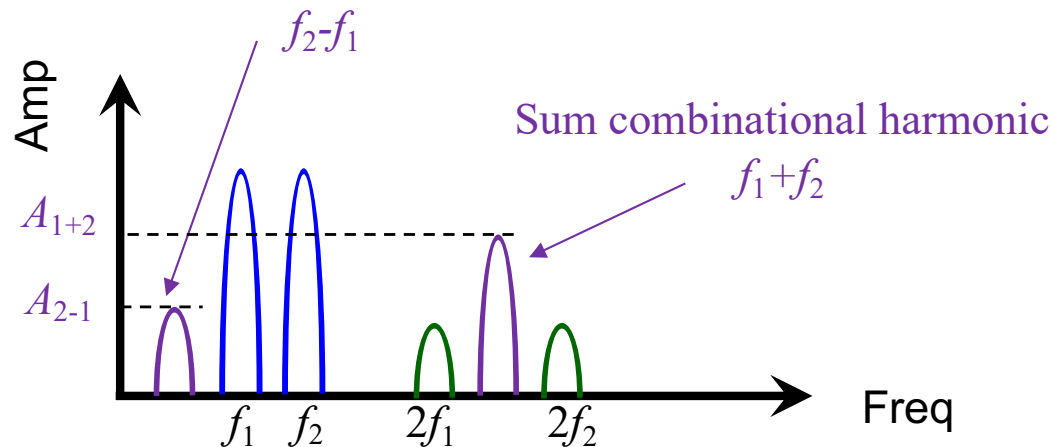
Superposition of original and phase reversed displacement field:

$$u(x, t)^{(0^\circ+180^\circ)} = -\frac{\beta x}{8c^2} \left\{ 2A_a^2 \omega_a^2 \cos 2(k_a x - \omega_a t) + 2A_b^2 \omega_b^2 \cos 2(k_b x - \omega_b t) \right. \\ \left. + 4A_a A_b \omega_a \omega_b \cos [(k_a + k_b)x - (\omega_a + \omega_b)t] \right. \\ \left. + 4A_a A_b \omega_a \omega_b \cos [(k_b - k_a)x - (\omega_b - \omega_a)t] \right\}$$

Second harmonics

Sum and difference combination harmonics

Difference combinational harmonic



$$\beta_{sum} = \frac{A_{1+2}}{A_1 A_2}$$

$$\beta_{diff} = \frac{A_{2-1}}{A_1 A_2}$$



# Experimental Studies

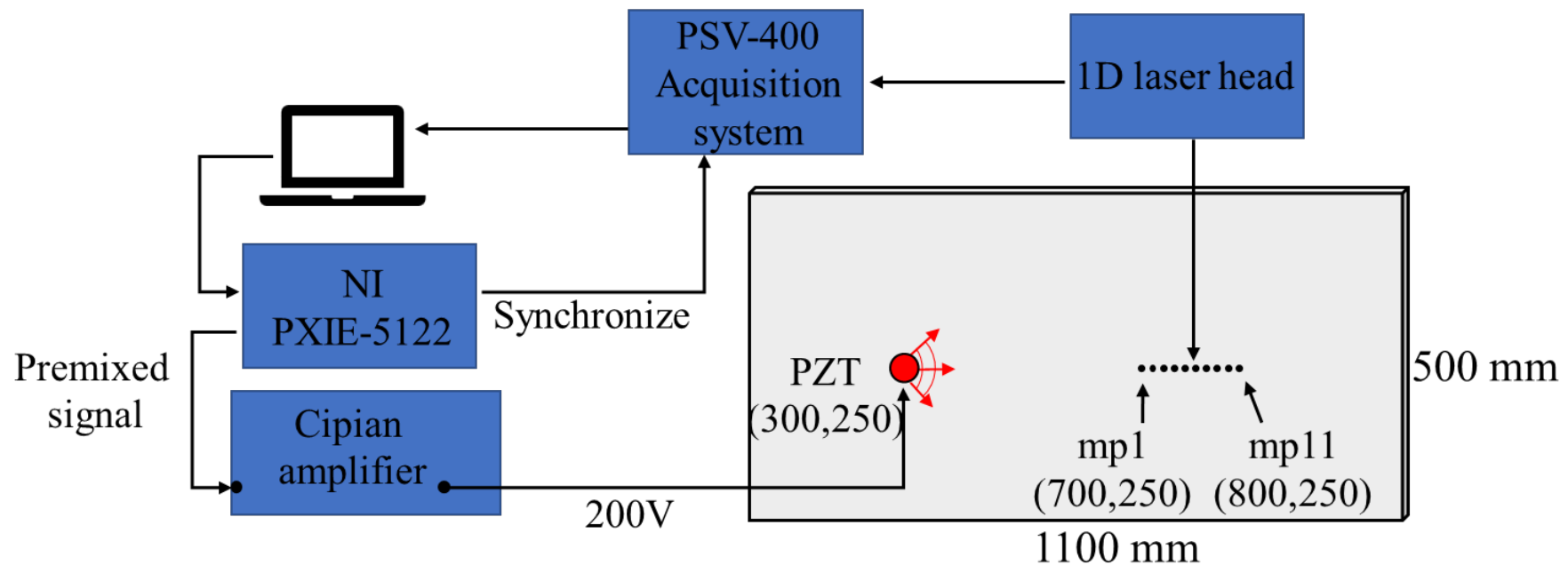
**Specimen:** 6061-T651 aluminium plate (1100mm x 500mm x 1.6mm)

**Guided wave mode:** Fundamental symmetric mode ( $S_0$ )

**Actuator:** Piezoelectric transducer, 10mm diameter, 0.5mm thick

**Excitation signal:** pre-mixing tone-burst pulse, the signal is amplified to 160V (peak-to-peak voltage)

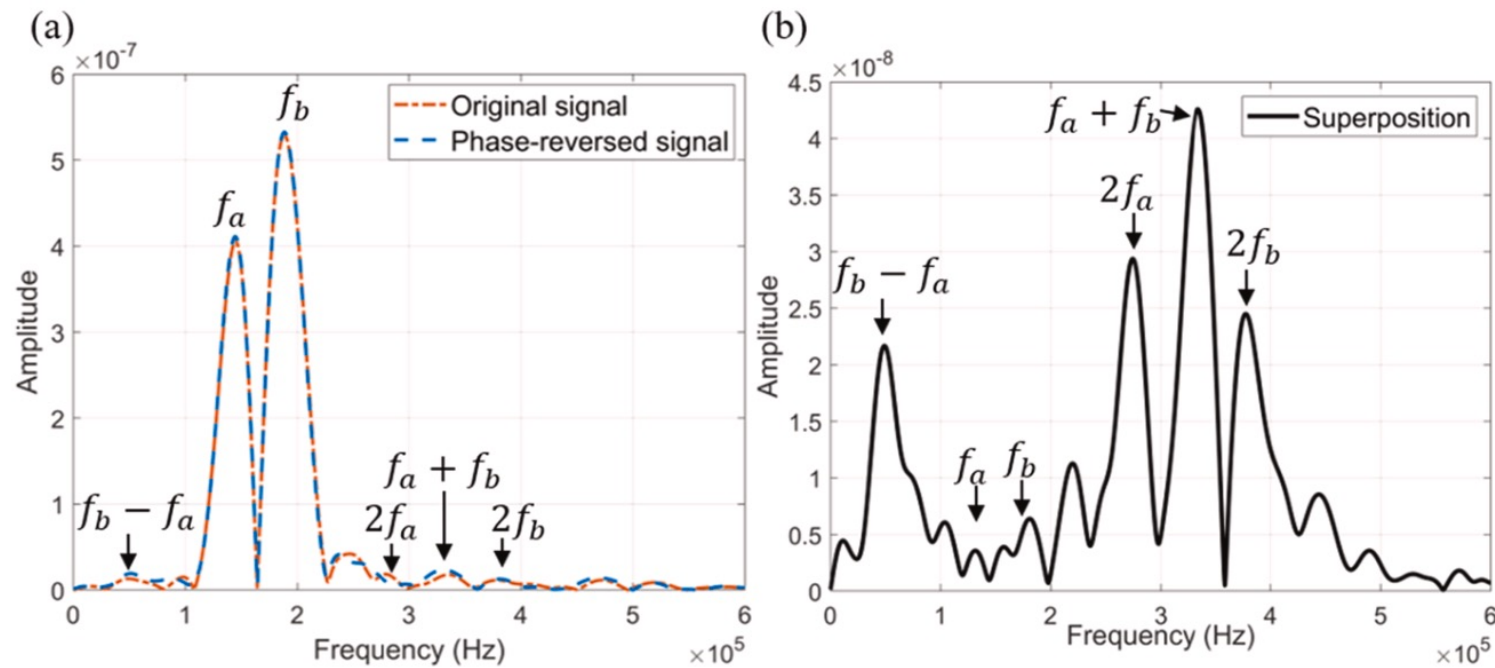
**Sensing:** 1D scanning laser vibrometer, 400mm from excitation, 10 measurement points with interval 10mm



# Experimental Studies

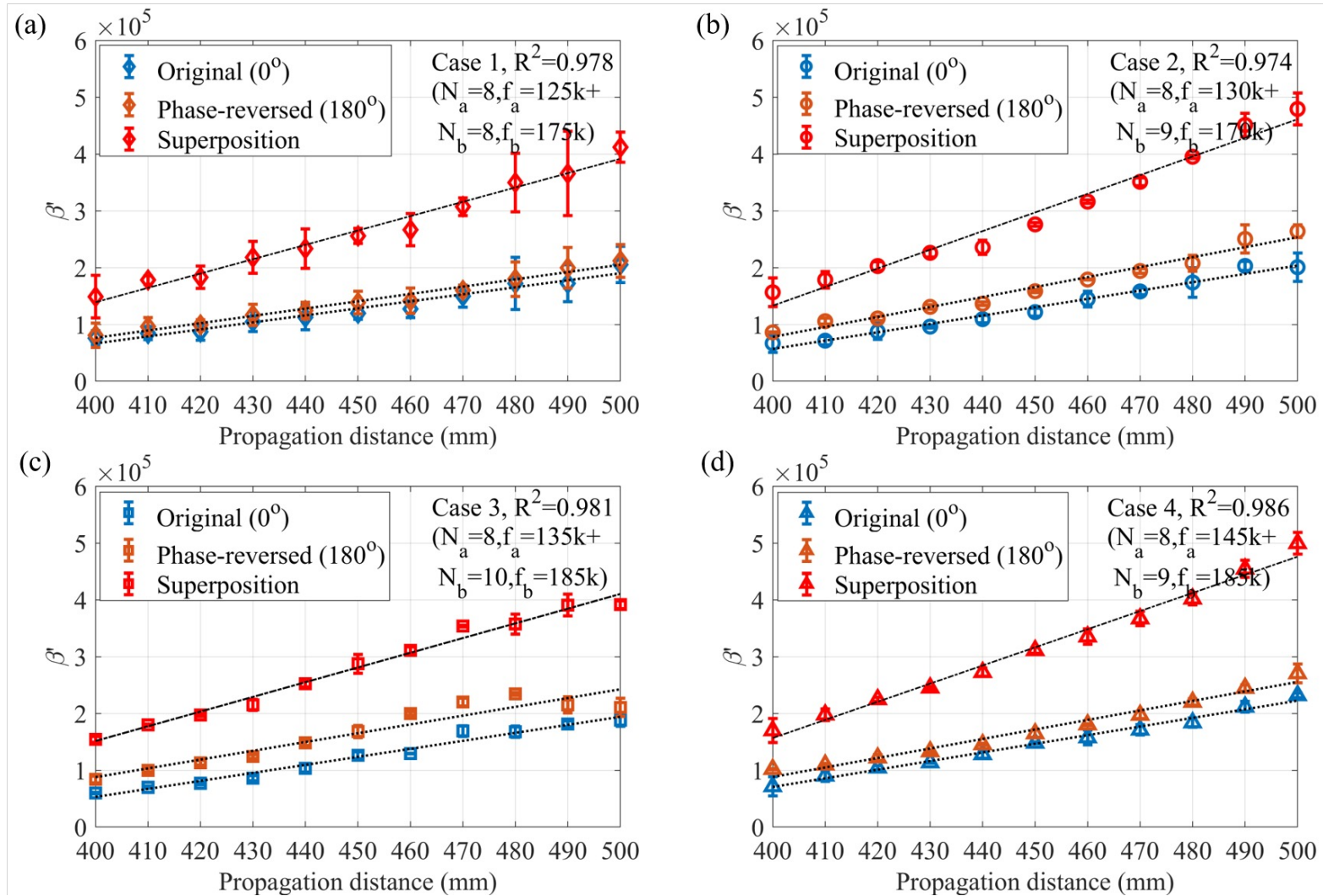
Different cases of wave mixing frequency pairs with varying excitation frequencies.

| Case | Fundamental frequency ( $f_a$ ) | Number of cycles ( $N_a$ ) | Fundamental frequency ( $f_b$ ) | Number of cycles ( $N_b$ ) |
|------|---------------------------------|----------------------------|---------------------------------|----------------------------|
| 1    | 125 kHz                         | 8 cycles                   | 175 kHz                         | 8 cycles                   |
| 2    | 130 kHz                         | 8 cycles                   | 170 kHz                         | 9 cycles                   |
| 3    | 135 kHz                         | 8 cycles                   | 185 kHz                         | 10 cycles                  |
| 4    | 145 kHz                         | 8 cycles                   | 185 kHz                         | 9 cycles                   |



Measured signal in the frequency domain of Case 4: a) original and phase reversed signal, and b) signal obtained after phase reversal

# Experimental Studies



Relative nonlinear parameters of sum combinational harmonic due to weak material nonlinearity, a) Case 1, b) Case 2, c) Case 3, and d) Case 4

# Experimental Studies

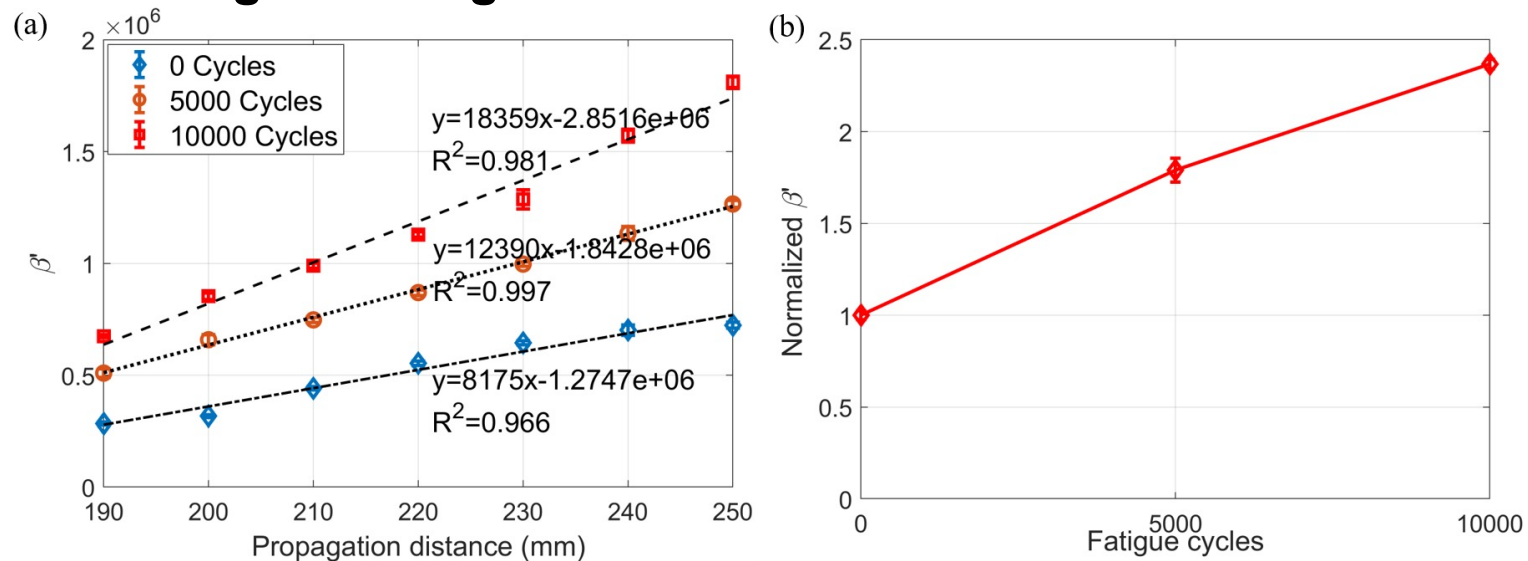
## Progressive fatigue damage

- Cyclic tensile loading
  - INSTRON 1242
  - Low cycle fatigue
  - Max. tensile loading = 90 kN (1.5Hz)
- Guided wave testing at:
  - 0 cycles
  - 5000 cycles
  - 10000 cycles
- Specimen fails at 12,417 cycles
  - Failure occurs in the bolting region (stress concentration)

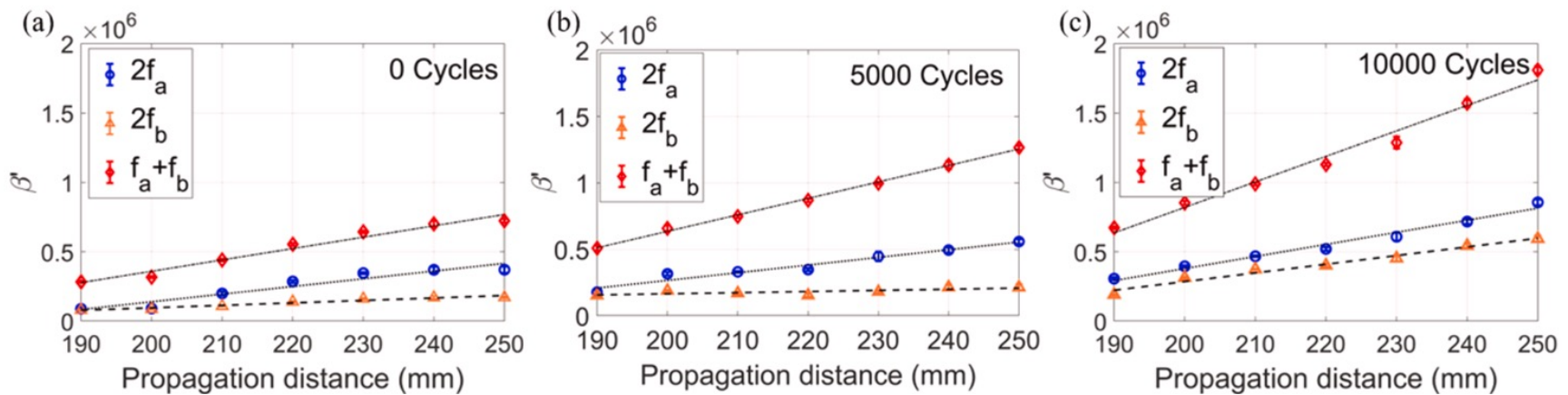


# Experimental Studies

## Progressive fatigue damage



Relative nonlinear parameters of sum combinational harmonic at different fatigue cycles



Combination harmonic vs second harmonic at different fatigue cycles

# Conclusions

- A guided wave mixing approach is demonstrated to provide early detection of fatigue damage
- The phase reversal approach is used to enhance the extraction of the nonlinear guided wave information
- Experimental results show that the combinational harmonics:
  - can be extracted robustly,
  - is sensitive to the early stage of fatigue damage,
  - can be used to monitor the fatigue damage, and
  - is more sensitive than second harmonic.

# Acknowledgements

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*Thank You*  
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